Density matrix – Problem 3

Suppose the density operator for a system at $t = 0$ is

$$\hat{\rho}(0) = Z^{-1}e^{-\beta\hat{H}}$$

where H is the system's Hamiltonian. Calculate $\hat{\rho}(t)$. What do you conclude about various properties of the system?